

EXPECTED RESPONSE AND SCORE	COMMENT
<p>ITEM 1: (10 SCORES)</p> <p>(a) Let the combined mean score and standard deviation be <math>\bar{X}_c</math> and <math>\delta_c</math> respectively</p> <p>For group A; <math>\sum x_A = 40 \times 65 = 2600</math> M1</p> <p>For group B; <math>\sum x_B = 60 \times 72 = 4320</math> M1</p> <p><math>n = n_A + n_B = 40 + 60 = 100</math></p> <p><math>\bar{X}_c = \frac{\sum x_A + \sum x_B}{n_A + n_B} = \frac{2600 + 4320}{100}</math> M1</p> <p><math>\bar{X}_c = 69.2</math> A1</p> <p>The combined mean of the students score is 69.2 B1</p> <p>Also; Combined standard deviation <math>\delta_c = \sqrt{\left(\frac{\sum x_A^2 + \sum x_B^2}{n_A + n_B}\right) - (\bar{X}_c)^2}</math></p> <p><math>\delta_c = \sqrt{\left(\frac{130000 + 358200}{100}\right) - (69.2)^2} = \sqrt{93.36}</math> M1</p> <p><math>\delta_c = 9.6623</math> A1</p> <p>The combined standard deviation of the students' score is 9.6623 B1</p> <p>(b) Arranging the scores in order of size</p> <p>54, 66, 73, 88, 92</p> <p>Lower quartile; <math>Q_1 = \frac{54 + 66}{2} = 60</math> M1</p> <p>Upper quartile; <math>Q_3 = \frac{88 + 92}{2} = 90</math> M1</p> <p>Interquartile range = <math>90 - 60 = 30</math></p> <p>The interquartile range of the students' score is 30 B1</p>	

**ITEM 2: (05 SCORES)**Resultant velocity vector =  $\mathbf{p} + \mathbf{q}$ 

$$\begin{pmatrix} 7 \\ -1 \end{pmatrix} = \begin{pmatrix} 3 \\ 4 \end{pmatrix} + \begin{pmatrix} x \\ y \end{pmatrix}$$

Horizontally;  $3 + x = 7$ 

$$x = 7 - 3 = 4$$

Vertically;  $4 + y = -1$ 

$$y = -1 - 4 = -5$$

Hence;  $\mathbf{q} = (4\mathbf{i} - 5\mathbf{j}) \text{ ms}^{-1}$ 

$$\begin{aligned} \text{Actual size of velocity vector } \mathbf{q} &= |\mathbf{q}| = \sqrt{(4)^2 + (-5)^2} \\ &= \sqrt{41} = 6.4031 \text{ ms}^{-1} \end{aligned}$$

The actual size of the velocity vector  $\mathbf{q}$  is  $6.4031 \text{ ms}^{-1}$ **ITEM 3: (05 SCORES)**Let  $R_A$  and  $R_B$  be the ranks of committee A and B respectively

$R_A$	6	2	4	1	5	8	3	7
$R_B$	1	3	7	8	4	5	2	6
$d$	5	-1	-3	-7	-1	3	1	1
$d^2$	25	1	9	49	1	9	1	1

$$\sum d^2 = 96$$

Using Spearman's rank correlation coefficient;  $r_s = 1 - \frac{6 \sum d^2}{n(n^2-1)}$ 

$$r_s = 1 - \frac{6 \times 96}{8(8^2-1)}$$

$$= -0.1429$$

The rank correlation coefficient between the results of the two committees is  $-0.1429$ **Interpretation/comment**There is a very low negative correlation between the results of the two committees.**Alternatively;**The players' blame towards their coach is not significant at both levels of significance based on 8 pairs of observations.

ITEM 4: (20 SCORES)

A frequency distribution table showing the weights in kg of 70 players B1

Weight (kg)	f	c.f	c	f/c	x	f.x
40 - 50	5	5	10	0.5	45	225
50 - 55	10	15	5	2.0	52.5	525
55 - 60	9	24	5	1.8	57.5	517.5
60 - 65	20	44	5	4.0	62.5	1250
65 - 70	6	50	5	1.2	67.5	405 <span style="float: right;">B1</span>
70 - 85	15	65	15	1.0	77.5	1162.5
85 - 90	5	70	5	1.0	87.5	437.5
SUM	70					4522.5 <span style="float: right;">B1</span>

(a) Average weight;  $\bar{X} = \frac{\sum fx}{\sum f} = \frac{4522.5}{70}$  M1

$\bar{X} = 64.6071$  kg A1

Since 64.6071 kg is less than 75 kg, the team doctor should introduce the food supplements. B1 B1

Popular weight of the players = modal weight/mode

Modal class is (60 - 65) since it has the highest frequency density of 4.0 B1 B1

Modal weight =  $l_0 + \left(\frac{d_1}{d_1 + d_2}\right) \times c$

=  $60 + \left(\frac{2.2}{2.2 + 2.8}\right) \times 5 = 62.2$  kg M1

The modal weight is 62.2 kg A1

Second quartile of the players' weight = median weight/middle weight

Median class is 60 - 65, located at the 35<sup>th</sup> position using cumulative frequency B1

Median weight =  $l_0 + \left(\frac{\frac{1}{2}N - cf_b}{f_m}\right) \times c$

=  $60 + \left(\frac{35 - 24}{20}\right) \times 5 = 62.75$  kg M1 A1

The second quartile of the players' weight is 62.75 kg B1

Since both the popular and second quartile of the players' weight are greater than 60 kg, the program can be considered positive. B1

ITEM 5: (20 SCORES)

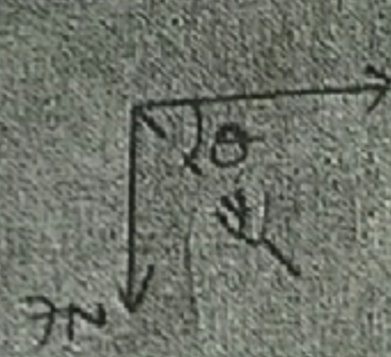
Item 5:

For student A

For forces in 2 dimensions

Resultant of forces =  $\underline{b} + \underline{c} + \underline{g} = \begin{pmatrix} 6 \\ -3 \end{pmatrix} + \begin{pmatrix} 3 \\ 1 \end{pmatrix} + \begin{pmatrix} -1 \\ -5 \end{pmatrix} = \begin{pmatrix} 8 \\ -7 \end{pmatrix} \text{ N}$

Size of resultant force =  $\sqrt{8^2 + (-7)^2} = \sqrt{113} = 10.6301 \text{ N}$

For direction  from  $\tan \theta = \frac{7}{8}$   
 $\theta = \tan^{-1}\left(\frac{7}{8}\right) = 41.19^\circ$

The size of the resultant force is 10.6301 N acting at  $41.19^\circ$  below the horizontal.

For forces in 3 dimensions

Resultant of forces =  $\underline{a} + \underline{c} + \underline{d} + \underline{e}$   
 $= \begin{pmatrix} 2 \\ 7 \\ 7 \end{pmatrix} + \begin{pmatrix} 0 \\ -4 \\ -3 \end{pmatrix} + \begin{pmatrix} 8 \\ 4 \\ 9 \end{pmatrix} + \begin{pmatrix} 2 \\ 3 \\ 4 \end{pmatrix} = \begin{pmatrix} 12 \\ 10 \\ 13 \end{pmatrix} \text{ N}$

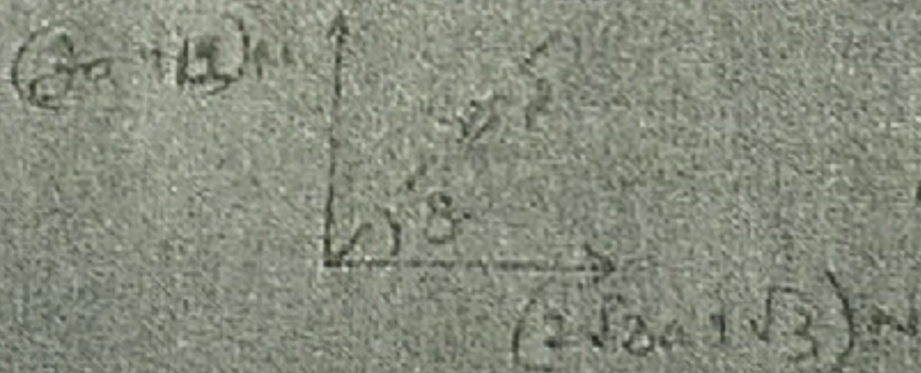
Modulus of resultant forces =  $\sqrt{12^2 + 10^2 + 13^2} = \sqrt{533} = 23.0868 \text{ N}$

The modulus of resultant of forces in 3 dimensions is 23.0868 N

For student B

Resultant force =  $\begin{pmatrix} \sqrt{3}a + 2\sqrt{3} \\ 8 \end{pmatrix} + \begin{pmatrix} 3\sqrt{3}a \\ 4a - 1 \end{pmatrix} + \begin{pmatrix} -\sqrt{3} \\ -a + 5 \end{pmatrix} = \begin{pmatrix} 2\sqrt{3}a + \sqrt{3} \\ 3a + 12 \end{pmatrix} \text{ N}$

From  $\theta = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$ ;  $\tan \theta = \frac{1}{\sqrt{3}}$



So  $\frac{3a + 12}{2\sqrt{3}a + \sqrt{3}} = \frac{1}{\sqrt{3}}$

$3a + 12 = 6a + \sqrt{3}$

$3a = 9$

$a = 3$

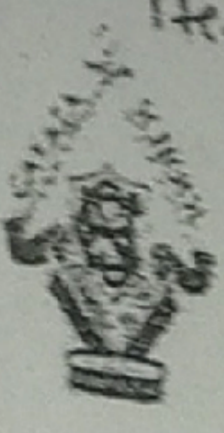
The value of 'a' = 3

Resultant force =  $\begin{pmatrix} 2\sqrt{3}(3) + \sqrt{3} \\ -3(3) + 12 \end{pmatrix} = \begin{pmatrix} 7\sqrt{3} \\ 21 \end{pmatrix}$

Size of resultant force =  $\sqrt{(7\sqrt{3})^2 + 21^2} = \sqrt{588} = 24.2487 \text{ N}$

The size of the single force with same effect of 3 forces = 24.2487 N

ITEM 6: (20 SCORES)



Item 6 (10/10)  
**GAYAZA HIGH SCHOOL**

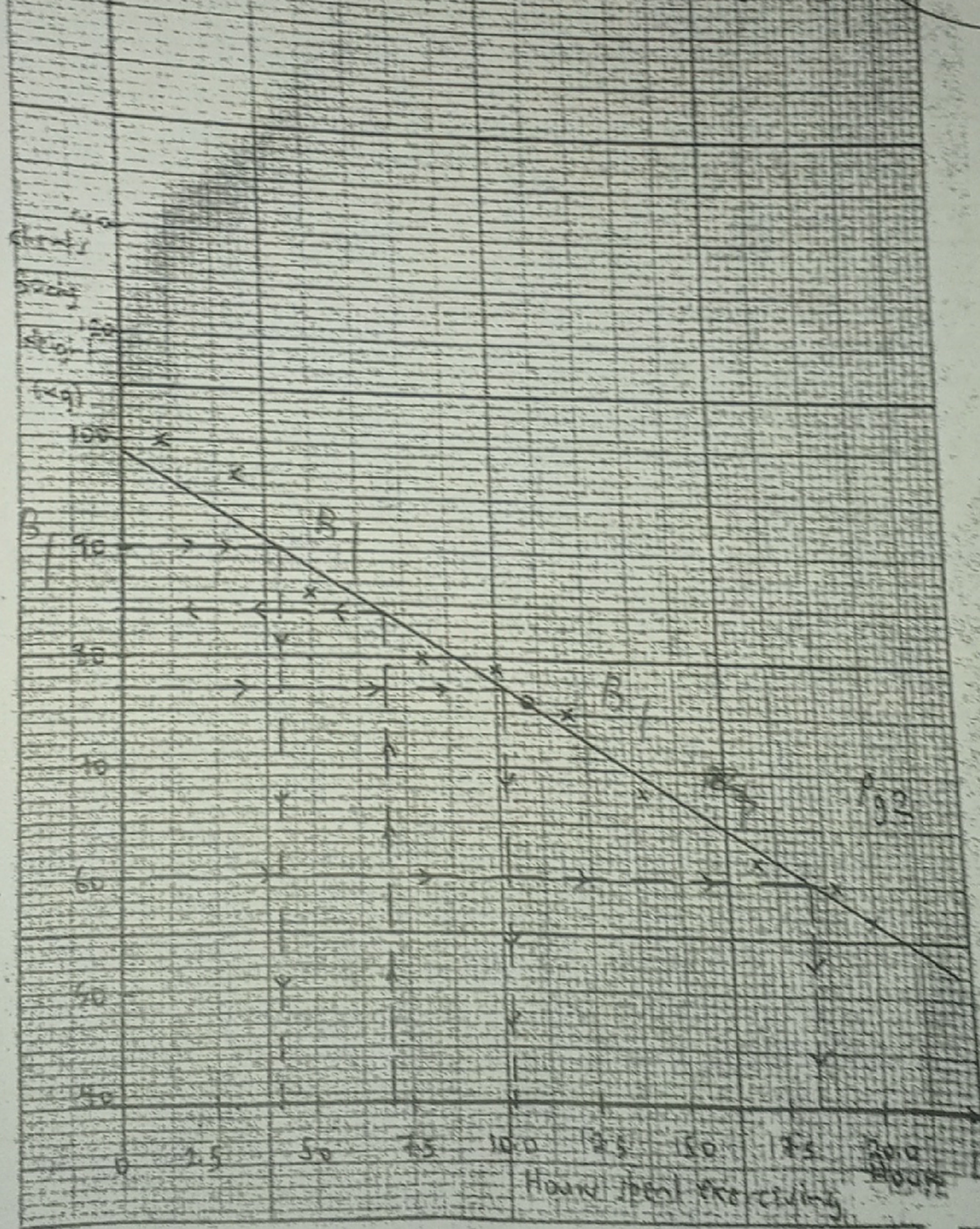
Student's Name \_\_\_\_\_

Signature \_\_\_\_\_

Subject Name Applied Mathematics Paper code P425/2

10/20

A scatter graph representing the data collected from a sample of households of Paradise Island City.



Item 6 (a)(vi)

Let the hours spent exercising =  $x$

Let the client's body weight (kg) =  $y$

$$\bar{x} = \frac{\sum x}{n}$$

$$\bar{x} = \frac{1+3+5+8+10+12+14+17+19+20}{10}$$

$$\bar{x} = \frac{109}{10}$$

$$\bar{x} = 10.9$$

$$\bar{y} = \frac{\sum y}{n}$$

$$= \frac{100+97+86+80+79+75+69+62+60+57}{10}$$

$$= \frac{764}{10}$$

$$\bar{y} = 76.4$$

$$(\bar{x}, \bar{y}) = (10.9, 76.4)$$

From the graph

Participant L who recorded a body weight of 77kg spent  $10.25 \pm 0.25$  hours ( $\pm 10$  hours)

OR

From the graph  $(4.125, 90)$ ,  $(19.375, 60)$

Gradient  $m = \frac{y_2 - y_1}{x_2 - x_1}$

$$= \frac{60 - 90}{19.375 - 4.125}$$

$$= \frac{-30}{14.25}$$

$$= -\frac{30}{14.25}$$

$$m = -\frac{40}{19}$$

At  $(4.125, 90)$   $y = mx + c$

$$90 = -\frac{40}{19} \times 4.125 + c$$

$$90 = -\frac{165}{19} + c$$

$$90 + \frac{165}{19} = c$$

$$c = \frac{1875}{19} \quad B$$

from  $y = mx + c$

$$y = \frac{-40x}{19} + \frac{1875}{19} \quad B$$

for  $x = 420$  minutes

number of hour

$$x = \frac{420}{60}$$

60

$$x = 7 \text{ hour} \quad B$$

$$y = \frac{-40 \times 7}{19} + \frac{1875}{19} \quad M$$

$$y = \frac{1595}{19} \text{ kg}$$

$$y = 83.9474 \text{ kg} \quad A$$

OR from the graph  $y = 84 \text{ kg} \pm 10 \text{ kg}$

Participant K who spent 420 minutes exercising had a body weight of 84 kg  $B$

from the equation for  $y = 77 \text{ kg}$

$$77 = \frac{-40x}{19} + \frac{1875}{19} \quad M$$

$$\frac{40x}{19} = \frac{1875}{19} - 77$$

$$\frac{40x}{19} = \frac{412}{19}$$

$$40x = 412$$

$$x = 10.3 \text{ hour} \quad A$$

(a) There is a negative relationship between the hours spent exercising and client's body weight. B

(b)

A table representing the data collected from a sample of participants. B

Participant	x	R <sub>x</sub>	y	R <sub>y</sub>	d = R <sub>x</sub> - R <sub>y</sub>	d <sup>2</sup>
A	1	10	100	1	9	81
B	3	9	97	2	7	49
C	5	8	86	3	5	25
D	8	7	80	4	3	9
E	10	6	79	5	1	1
F	12	5	75	6	1	1
G	14	4	68	7	-3	9
H	17	3	62	8	-5	25
I	19	2	60	9	-7	49
J	20	1	57	10	-9	81
					$\Sigma d = 330$	

$$r = \frac{1}{n} \frac{\sum d^2}{(n^2 - 1)}$$

$$= \frac{1}{10} \frac{6 \times 330}{(10^2 - 1)}$$

$$= \frac{1}{10} \frac{1980}{990}$$

$$r = -1$$

There is a negative high correlation between hours spent exercising and client's body weight. B  
 Since there is a negative relationship, the management will not increase on the hours the clients spend exercising since the management can only increase the hours if there's a positive relationship. B

END

P35